

KATWA COLLEGE
SEM-I MAJOR
INTERNAL ASSESSMENT EXAMINATION-2023
SUBJECT: PHYSICS
PAPER CODE: PHYS1011

Time: 1h

FM-15

Answer any three questions:

- a) If \vec{r} is the position vector of a point then show that the $\text{div} (r^4 \vec{r}) = 7r^4$.
Show that $r^n \vec{r}$ is irrotational vector.
- b) If $f(x, y) = 0$ and $\varphi(y, z) = 0$. Show that $\frac{\partial f}{\partial y} \frac{\partial \varphi}{\partial z} \frac{dz}{dx} = \frac{\partial f}{\partial x} \frac{\partial \varphi}{\partial y}$.
Solve $(1+xy)ydx + (1-xy)x dy = 0$
- c) Show that linearly independent solutions of $y'' - 3y' + 2y = 0$ are e^x and e^{2x} . Find the solution of $y(x)$ with the property that $y(0) = 0$, $y'(0) = 1$.
- d) Prove that cylindrical coordinate system is orthogonal.
- e) Solve : $y'' - y' - 2y = \sin 2x$